

MA 161 ONLINE, SUMMER 2026

Quiz 10: §5.2, 5.3

Name: Key
PUID: _____

Score: _____/20
Length: 15 minutes

Directions: Follow these instructions carefully. Failure to do so may result in your quiz being invalidated and/or an academic integrity violation. All suspected violations of academic integrity will be reported to the Office of the Dean of Students.

- Complete each question below. There are 3 questions; the maximum score is 20 points.
- You have 25 minutes: 15 minutes to complete the quiz and 10 minutes to upload it to Gradescope.
- This quiz is closed book and closed notes. Calculators are not allowed.
- You are to work independently. External help (including, but not limited to, using the internet and generative AI) is prohibited.
- You may use your own paper to complete this quiz; you do not need to print this document.
- Adequate work must be shown for each problem. A question with little to no work, even with a correct answer, will result in a low score.
- Make sure your work is neat and legible, especially after it is scanned. Use proper notation, and clearly mark the question numbers and your final answer. Points may be taken off if part of your work is unreadable.

(The questions start on the next page, one problem per page)

1. The **error function** $\text{erf}(x)$ is defined using an integral:

$$\text{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$$

(a) [5 points] Show $\int_{-1}^3 e^{-t^2} dt = \frac{\sqrt{\pi}}{2} [\text{erf}(3) - \text{erf}(-1)]$ by combining the right hand side into one integral.

$$\begin{aligned} \frac{\sqrt{\pi}}{2} [\text{erf}(3) - \text{erf}(-1)] &= \frac{\sqrt{\pi}}{2} \left[\frac{2}{\sqrt{\pi}} \int_0^3 e^{-t^2} dt - \frac{2}{\sqrt{\pi}} \int_0^{-1} e^{-t^2} dt \right] \\ &= \int_0^3 e^{-t^2} dt - \int_0^{-1} e^{-t^2} dt = \int_0^3 e^{-t^2} dt + \int_{-1}^0 e^{-t^2} dt \\ &= \int_{-1}^3 e^{-t^2} dt \end{aligned}$$

(b) [5 points] Find $\frac{dy}{dx}$ if $y = \text{erf}(x^2)$

$$\frac{dy}{dx} = \frac{d}{dx^2} \text{erf}(x^2) \cdot \frac{d}{dx} (x^2)$$

$$\xrightarrow{\text{FTC}} \left(\frac{2}{\sqrt{\pi}} e^{-(x^2)^2} \right) (2x) = \frac{4}{\sqrt{\pi}} x e^{-x^4}$$

2. [9 points] Evaluate the integral:

$$\int_1^2 \frac{4+u^2}{u^3} du$$

$$\int_1^2 \frac{4+u^2}{u^3} du = \int_1^2 \left(\frac{4}{u^3} + \frac{1}{u} \right) du = \int_1^2 (4u^{-3} + u^{-1}) du$$

$$\underline{\underline{\text{FTC}}} \left[\frac{4}{-2} u^{-2} + \ln|u| \right]_1^2$$

$$= \left[\frac{-2}{u^2} + \ln|u| \right]_1^2$$

$$= \left[\left(-\frac{1}{2} + \ln 2 \right) - \left(-2 + \ln 1 \right) \right]$$

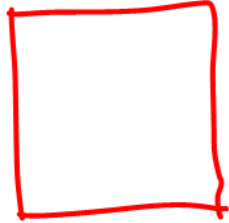
$$= 2 - \frac{1}{2} + \ln 2$$

$$= \frac{3}{2} + \ln 2$$

3. [1 point] Final quiz question of the semester: What's $2 + 2$?

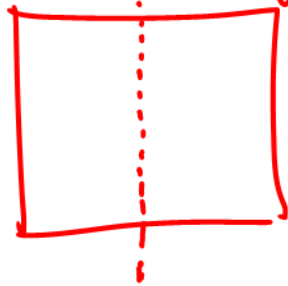
(Answers that attempt to make the grader laugh are highly encouraged.)

4, but where is the fun without a silly and needlessly convoluted explanation. Given a square



We count in two ways the number of ways of selecting a corner. The total number of corners is 4, hence there are 4 ways we can choose a corner.

However, split the square in half



There are 2 ways of selecting a corner left of the divider, and 2 ways of selecting a corner to the right of the divider.

Thus, there are $2+2$ ways of selecting a corner of the square. Therefore,

$$4 = 2 + 2$$